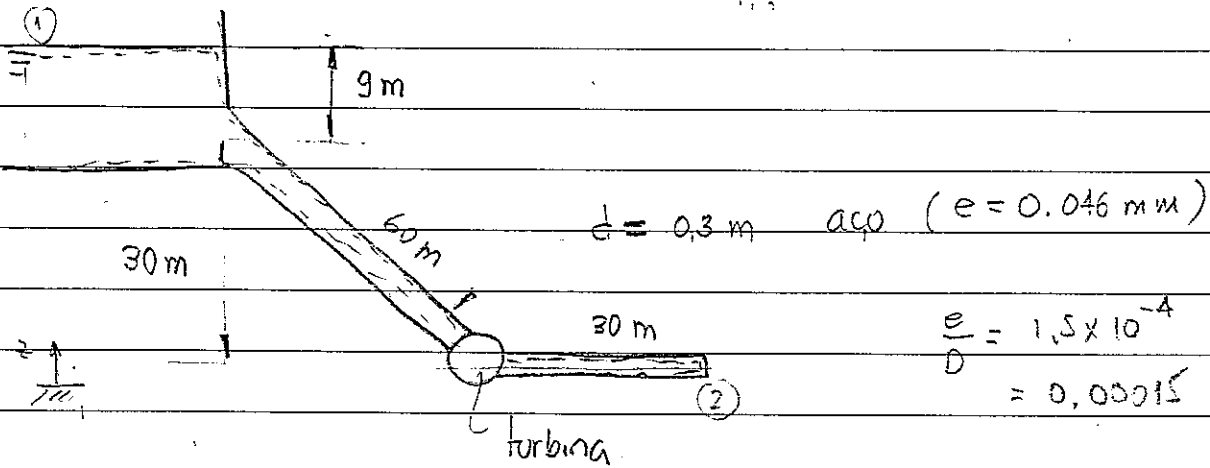




Prob. 8.36 shames

Água move a turbina produzindo 75 kW. Qual a vazão?



eq da energia:

$$\left( \frac{p_1}{\rho} + \alpha_1 \frac{V_1^2}{2} + g z_1 \right) - \frac{\dot{W}_{\text{tubo}}}{\dot{m}} - \left( \frac{p_2}{\rho} + \alpha_2 \frac{V_2^2}{2} + g z_2 \right) = h_{fT}$$

$$p_1 = p_{atm} = p_2$$

$$V_1 \approx 0$$

$$\alpha_2 \approx 1$$

$$z_2 = 0$$

$$\left( \frac{p_{atm}}{\rho} + \alpha_1 \frac{V_1^2}{2} + g z_1 \right) - \frac{\dot{W}_{\text{TUBO}}}{\dot{m}} - \left( \frac{p_{atm}}{\rho} + \frac{V_2^2}{2} + g z_2 \right) = h_f + h_{fT}$$

$$h_f = f \frac{L}{D} \frac{V^2}{2}$$

$$\dot{m} = \rho A V$$

$$g z_1 - \frac{\dot{W}_{\text{TURB}}}{\dot{m}} - \frac{V^2}{2} = f \frac{L}{D} \frac{V^2}{2}$$

$$g z_1 = \left( \frac{f L}{2 D} + \frac{1}{2} \right) V^2 + \frac{\dot{W}_T}{\rho A V}$$

$$g z_1 \rho A V = \left( \frac{f L}{2 D} + \frac{1}{2} \right) V^3 \rho A + \dot{W}_T$$

$$\left( \frac{f L}{2 D} + \frac{1}{2} \right) V^3 \rho A + \dot{W}_T - g z_1 \rho A V = 0$$

$$\rho A \left[ \frac{f L}{2 D} + \frac{1}{2} \right] V^3 - \rho g A V + \dot{W}_T = 0$$

$$(1000) (\pi) (0.3)^2 \left[ \frac{f (60+30)}{4 (2)(0.3)} + \frac{1}{2} \right] V^3 - (9.8) (30+9) (1000) (\pi) (0.3)^2 V + 75 \times 10^3 = 0$$

$$(70.69) \left[ f (150) + \frac{1}{2} \right] V^3 - (2.7 \times 10^4) V + 75 \times 10^3 = 0$$

$$\left[ (1.06 \times 10^4) f + (35.35) \right] V^3 - (2.7 \times 10^4) V + 75 \times 10^3 = 0$$

1) chute  $f = 0.02$  obtém  $V = 3.033 \text{ m/s}$

calcula  $Re = \frac{\rho V D}{\mu} = \frac{(1000)(3.033)(0.3)}{10^{-3}} = 9 \times 10^5$

do diagrama de Moody para  $e/D = 0.00015 \rightarrow f = 0.014$

2) obtém  $V = 2.953 \text{ m/s}$   $\therefore Re = 8.86 \times 10^5 \rightarrow f = 0.014 \text{ ok!}$

Assim,  $V = 2.95 \text{ m/s}$

$$Q = VA = (2.95) (\pi) \frac{(0.3)^2}{4} = 0.21 \text{ m}^3/\text{s}$$